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STATEMENT OF A PROBLEM OF A TWO-LINKED ROBOT MOVEMENT OPTIMIZATION

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The first step in the statement of a problem is to describe a robot under consideration. Its scheme is presented in fig.1.

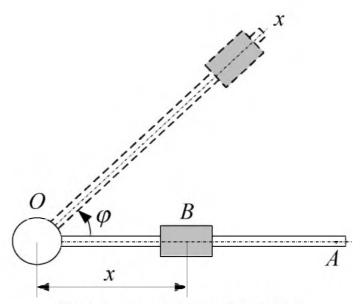


Fig. 1. Scheme of the two-linked robot

Mathematical model of system motion is as follows:

$$\begin{cases}
M - M_{cm} = \frac{d}{dt} [(J_0 + mx^2)\dot{\phi}]; \\
F - F_{cm} = m\ddot{x} - m\dot{\phi}^2 x,
\end{cases}$$
(1)

where x - the distance from the point O to the center of inertia B, J_0 - the total moment of inertia A and B for the axis O (when x=0), M - torque that rotates the bodies A and B; M_{cm} - static torque of resistance that impacts the rotation of the system; φ - the angular coordinate of body A; F - driving force that impacts the body

 \mathbf{B} ; F_{cm} - the force of static resistance that impacts the body \mathbf{B} ; m - the mass of the body \mathbf{B} .

The criterion to minimize is an integral functional, which determines the weighted sum of the root mean square values of dynamic components of the driving force of the torque:

$$I_{j} + \delta I_{F} = \int_{0}^{t_{1}} (M - M_{\tilde{n}\dot{o}})^{2} dt + \delta \int_{0}^{t_{1}} (F - F_{\tilde{n}\dot{o}})^{2} dt =$$

$$= \int_{0}^{t_{1}} ((J_{0} + mx^{2})\ddot{\phi} + 2mx\dot{x}\dot{\phi})^{2} + \delta (m\ddot{x} - m\dot{\phi}^{2}x)^{2} dt \rightarrow \min,$$
(2)

where δ - the weight that reduces the measurement of the forces to torque (Nm) and takes into consideration the significance of the RMS force minimization; t_1 – duration of the controlled mode. A dot under character denotes the derivative on time.

The next step in the statement of the optimal control problem is to write down the boundary conditions of the system movement:

$$\begin{cases}
\varphi(0) = \dot{\varphi}(0) = 0, & \tilde{o}(0) = \tilde{o}_0, & \tilde{o}(0) = 0; \\
\varphi(t_1) = \varphi_{t_1}, & \dot{\varphi}(t_1) = 0, & \tilde{o}(t_1) = \tilde{o}_1, & \tilde{o}(t_1) = 0, & \varphi \in [0, \pi],
\end{cases}$$
(3)

where x_0 and x_1 – the initial and the final position of the body \boldsymbol{B} ; φ_{t_1} - the final position of the link \boldsymbol{A} .

The stated optimal control problem should be solved in further investigations.